

Different pathways for activation and deactivation in $Ca_v1.2$: a minimal gating model

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Point mutations in pore-lining S6 segments of $Ca_v1.2$ shift the voltage dependence of activation into the hyperpolarizing direction and significantly decelerate current activation and deactivation. Here, we analyze these changes in channel gating in terms of a circular four-state model accounting for an activation R–A–O and a deactivation O–D–R pathway. Transitions between resting-closed (R) and activated-closed (A) states (rate constants $x(V)$ and $y(V)$) and open (O) and deactivated-open (D) states ($u(V)$ and $w(V)$) describe voltage-dependent sensor movements. Voltage-independent pore openings and closures during activation (A–O) and deactivation (D–R) are described by rate constants α and β , and γ and δ , respectively. Rate constants were determined for 16-channel constructs assuming that pore mutations in IIS6 do not affect the activating transition of the voltage-sensing machinery ($x(V)$ and $y(V)$). Estimated model parameters of 15 $Ca_v1.2$ constructs well describe the activation and deactivation processes. Voltage dependence of the “pore-releasing” sensor movement ($x(V)$) was much weaker than the voltage dependence of “pore-locking” sensor movement ($y(V)$). Our data suggest that changes in membrane voltage are more efficient in closing than in opening $Ca_v1.2$. The model failed to reproduce current kinetics of mutation A780P that was, however, accurately fitted with individually adjusted $x(V)$ and $y(V)$. We speculate that structural changes induced by a proline substitution in this position may disturb the voltage-sensing domain.

INTRODUCTION

The pore-forming α_1 subunits of Ca channels (Ca_v) are composed of four homologous domains (I–IV) formed by six transmembrane segments (S1–S6) that are linked together on a single polypeptide (Catterall, 2000). In analogy to potassium channels (Doyle et al., 1998; Zhou et al., 2001; Jiang et al., 2002; Long et al., 2005; Swartz, 2005; Tombola et al., 2006), it is assumed that S6 segments line the channel pore, with an S6 bundle-crossing region in the lower third forming the channel gate. Unlike potassium channels, which are composed of four identical units, Ca_v are asymmetric. None of the four S6 segments carries a PXP motif like Shaker, and a conserved G89 in MthK (Jiang et al., 2003) is present only in segments IS6 and IIS6.

We have recently identified a motif of hydrophobic residues in the lower third of segment IIS6 that is conserved in high voltage-activated $Ca_v1.2$ and plays an important role in activation gating (779–782: LAIA; see Hemara-Wahanui et al., 2005; Hohaus et al., 2005). Replacement of these IIS6 residues by amino acids of different hydrophobicity, size, and polarity induced pronounced changes in channel gating, such as shifts in

the voltage dependence of activation, slow activation kinetics near the footstep of the activation curve, slow deactivation at all potentials, and decreased inactivation (for review see Hering et al., 2008 and Stary et al., 2008). In continuation of these studies, we substituted residues in the lower third of segment IIS6 by flexible glycines. In line with our previous data, these mutations induced remarkable shifts of the activation curve to hyperpolarized voltages and characteristic slowing of the activation and deactivation kinetics. Shifts of the activation curve can be interpreted as destabilization of the closed state and/or as stabilization of the open-channel conformation (Yifrach and MacKinnon, 2002; Zhao et al., 2004).

To distinguish between these possibilities, we analyzed changes in steady-state activation and current kinetics in terms of a four-state model where activation and deactivation may occur predominantly via different pathways (see Fig. 1). Under the assumption that pore mutations in IIS6 do not affect the activating transition of the voltage-sensing machinery ($x(V)$, $y(V)$) (Yifrach and MacKinnon, 2002), rate constants for 16 $Ca_v1.2$ constructs were estimated by means of an inverse problem

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Abbreviation used in this paper: ODE, ordinary differential equation.

approach (see Engl et al., 1996). Satisfactory fits for 15 out of 16 channel constructs were achieved assuming a single pair of $x(V)$ and $y(V)$. These results suggest that most of the analyzed structural changes in IIS6 do not significantly affect the voltage-sensing domain. Fitting the kinetics of mutant A780P required individual adjustment of $x(V)$ and $y(V)$, suggesting that stiff helix kinking in this position may affect voltage sensor movements.

MATERIALS AND METHODS

Experimental procedures

Mutagenesis. The $\text{Ca}_v1.2$ α_1 subunit coding sequence (GenBank accession no. X15539) in-frame 3' to the coding region of a modified green fluorescent protein was provided by M. Grabner (Innsbruck Medical University, Innsbruck, Austria) (Grabner et al., 1998). For electrophysiological studies, we used the plasmid lacking the green fluorescent protein tag. Glycine mutations (A780G, I781G, A782G, V783G, and D784G) in segment IIS6 of the $\text{Ca}_v1.2$ α_1 subunit were introduced by the "gene SOEing" technique (Horton et al., 1989). The mutated fragments were cloned into a BamHI-AflIII cassette (nt 1,265 and 2,689; numbering according to the $\text{Ca}_v1.2$ α_1 subunit coding sequence). All constructs were checked by restriction site mapping and sequencing.

Cell culture and transient transfection. Human embryonic kidney tsA-201 cells were grown at 5% CO_2 and 37°C to 80% confluence in Dulbecco's modified Eagle's/F-12 medium supplemented with 10% (vol/vol) fetal calf serum and 100 U/ml penicillin/streptomycin. Cells were split using trypsin/EDTA and plated on 35-mm Petri dishes (Falcon) at 30–50% confluence ~16 h before transfection. Subsequently, tsA-201 cells were cotransfected with cDNAs encoding wild-type or mutant $\text{Ca}_v1.2$ α_1 subunits with auxiliary β_{1a} as well as $\alpha_2\text{-}\delta_1$ subunits. Transfection of tsA-201 cells was done using the FUGENE6 Transfection Reagent (Roche) according to standard protocols.

Ionic current recordings and data acquisition. Barium currents (I_{Ba}) through voltage-gated Ca^{2+} channels were recorded at 22–25°C using the patch clamp technique (Hamill et al., 1981) with an Axopatch 200A patch clamp amplifier (MDS Analytical Technologies) 36–48 h after transfection. The extracellular bath solution contained 5 mM BaCl_2 , 1 mM MgCl_2 , 10 mM HEPES, and 140 mM choline-Cl, titrated to pH 7.4 with methanesulfonic acid. Patch pipettes with resistances of 1 to 4 M Ω were made from borosili-

cate glass (Clark Electromedical Instruments) and filled with pipette solution containing 145 mM CsCl, 3 mM MgCl_2 , 10 mM HEPES, and 10 mM EGTA, titrated to pH 7.25 with CsOH. All data were digitized using a DIGIDATA 1200 interface (MDS Analytical Technologies), smoothed by means of a four-pole Bessel filter and stored on computer hard disk. 100-ms current traces were sampled at 10 kHz and filtered at 5 kHz. For the steady-state inactivation protocol, currents were sampled at 1 kHz and filtered at 0.5 kHz, and tail currents were sampled at 50 kHz and filtered at 10 kHz. Leak currents were subtracted digitally using average values of scaled leakage currents elicited by a 10-mV hyperpolarizing pulse or electronically by means of an Axopatch 200 amplifier (MDS Analytical Technologies). Capacity currents were not subtracted. When the pipettes were filled with pipette solution, their input resistance ranged between 1 and 4 M Ω . The mean cell capacity was 31 ± 4 pF ($n = 15$). The mean series resistance was 4.9 ± 2.1 M Ω . It was compensated (60–85% compensation) by the following procedure: the depth of the positive feedback was gradually increased until oscillations (small overcompensation) appear. Even in large cells, the time constant of the capacity current (τ_{capacity}) did not exceed ≈ 0.25 ms (4 M Ω * 60 pF = 240 μ s). The early current phase was excluded from data processing (at least $3 * \tau_{\text{capacity}} \approx 0.75$ ms), and hyperpolarizing voltages < -100 mV were not applied.

Data processing

The pClamp software package (version 7.0; MDS Analytical Technologies) was used for data acquisition and preliminary analysis. Microcal Origin 5.0 was used for fitting the steady-state activation (m_∞) curves and time constants of current activation and deactivation. The voltage dependence of activation was determined from I-V curves that were fitted according to the following modified Boltzmann distribution:

$$I = \frac{G_{\text{max}} \cdot (V - V_{\text{rev}})}{1 + \exp\left(\frac{V_m - V}{k_s}\right)},$$

where V is membrane potential, I is peak current, G_{max} is maximum membrane conductance, V_{rev} is extrapolated reversal potential, V_m is voltage for half-maximal activation, and k_s is slope factor. The time course of current activation was fitted to a monoexponential function:

$$I(t) = a_0 \cdot \exp\left(-\frac{t}{\tau}\right) + C,$$

where $I(t)$ is current at time t , a_0 is the amplitude coefficient, τ is time constant, and C is a constant. Data are given as mean \pm standard

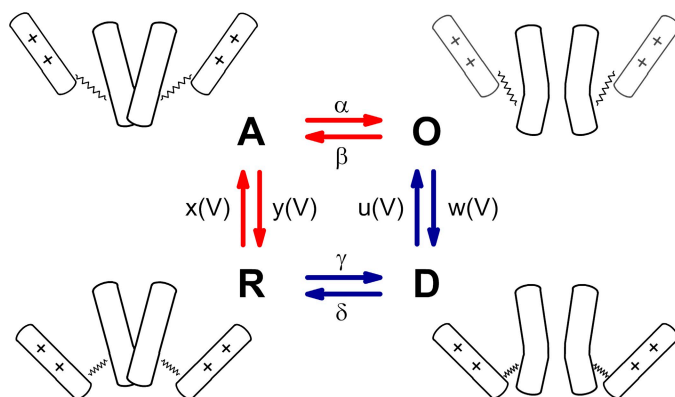


Figure 1. Schematic representation of $\text{Ca}_v1.2$ state transitions during activation. Activation gating assumed to be determined by two functionally separate processes: a voltage-sensing mechanism (++) and the conducting pore. Each functional unit can dwell in two states: the voltage sensor in the resting (down) and activated (up) states, and the pore in the open or closed states. The entire molecule therefore dwells in $2 \times 2 = 4$ states: R, pore is closed and voltage-sensing mechanism locks the pore; A, voltage-sensing mechanism is activated and releases the pore, which, however, remains closed; O, the pore is open; D, the deactivated voltage-sensing mechanism is in the down position while the pore is still open. The activation pathway is marked by red and the deactivation pathway by blue arrows. Rate constants of the pore opening and closure (α , β , γ , and δ) are assumed to be independent of the voltage. Rate constants of voltage-sensing mechanism (x , y , u , and w) are voltage dependent.

error, from which the time constant τ was determined. These voltage dependencies of the steady-state activation and time constants of activation and deactivation were then used as data for the identification of the parameters of a four-state model (see Fig. 1).

Inverse problem approach for the identification of model parameters

Given a guess for the model parameters α , β (describing the pore opening and closure during activation), γ , and δ (describing the pore opening and closure during deactivation), and x_0 , y_0 , k_x , and k_s (describing the voltage-sensing machinery), the above mentioned experimental data, i.e., steady-state activation and time constants, can be numerically simulated by means of the formulae (Eqs. 4.2 and 4.5) of the Results section. This task would be referred to as the direct problem. For solving the corresponding inverse problem of identifying the model parameters

$$q = (x_0, y_0, k_x, k_s, \alpha, \beta, \gamma, \delta)$$

from the experimental data, we followed a regularization approach (Engl et al., 1996). Instead of purely minimizing the mismatch between data and simulation over a set of admissible parameters, we considered the minimization of a Tikhonov-type objective functional consisting of a mismatch and a penalty term, i.e.,

$$\|data - simulation(q)\|^2 + \eta \|q - q_0\|^2 \rightarrow \min. \quad (1.1)$$

Parameter identification is inherently ill-conditioned in the sense that minimizers of the pure mismatch term (i.e., $\eta = 0$) do not depend on the data in a stable manner, such that even small measurement errors (inevitable in practice) may lead to severe errors in the computed parameters. The purpose of the penalty term $\eta \|q - q_0\|^2$ with $\eta > 0$ (where q_0 denotes an available a priori guess and $\|\cdot\|$ denotes the Euclidean norm) is to counteract the ill-conditioning of the problem, such that strong data error amplifications are avoided. Hence, the regularization parameter η acts as a balance between accuracy and stability; theoretical guidelines for its choice in dependency on the data noise level are given in Engl et al. (1996).

For describing the mismatch, we used a standard weighted least-squares formulation, i.e.,

$$\|data - simulation(q)\|^2 = \sum_i w_{act,i} (\tau_i^{data} - \tau_i^{sim}(q))^2 + \sum_k w_{\infty,k} (m_{\infty,k}^{data} - m_{\infty,k}^{sim}(q))^2, \quad (1.2)$$

with weights

$$w_{act,i} = 1 / (\tau_i^{data})^2, w_{\infty,k} = 1 / (m_{\infty,k}^{data})^2,$$

where the summation indices i and k reflect the fact that the data were collected at various voltage values $V_{tau,j}$ and $V_{\infty,k}$.

In case of simultaneous considerations of datasets, for several mutants the mismatch term simply is changed to

$$\sum_l \|data^l - simulation(q^l)\|^2,$$

with $data^l$ and parameters q^l corresponding to the mutant labeled by index l ; similarly, the penalty term of the Tikhonov functional is adapted.

The set of admissible parameters within a solution is sought for is defined via the restriction

$$5 \text{ mV} \leq \frac{k_x k_y}{k_x + k_y} \leq 10 \text{ mV}, \quad (1.3)$$

which reflects the finding that the slope (see Eq. 4.4 for the relation between k_y and k_x, k_s) of the activation curve ranged between 5.7 and 9.8 mV (see Table I). In addition, the constraint

$$2 \leq \frac{x_0}{y_0} \leq 5 \quad (1.4)$$

is derived from the observation that the activation curve was never shifted beyond -10 mV.

We also constrained the ratio between the fractions of activated open channels $F_{open,max}$ and spontaneously open channels at rest $F_{open,min}$:

$$F_{open,max} > 10 \cdot F_{open,min}. \quad (1.5)$$

Finally, we also considered the box constraints

$$\begin{aligned} 0.1 \text{ ms}^{-1} &\leq x_0 \leq 10 \text{ ms}^{-1}, \\ 0.1 \text{ ms}^{-1} &\leq y_0 \leq 2 \text{ ms}^{-1}, \\ 10 \text{ mV} &\leq k_x \leq 400 \text{ mV}, \\ 5 \text{ mV} &\leq k_y \leq 40 \text{ mV}, \\ 10^{-5} \text{ ms}^{-1} &\leq \alpha \leq 20 \text{ ms}^{-1}, \\ 10^{-5} \text{ ms}^{-1} &\leq \beta \leq 10 \text{ ms}^{-1}, \\ 10^{-5} \text{ ms}^{-1} &\leq \gamma \leq 1 \text{ ms}^{-1}, \\ 10^{-5} \text{ ms}^{-1} &\leq \delta \leq 5 \text{ ms}^{-1}, \end{aligned}$$

which were determined by preliminary simulations of current kinetics and steady-state activation curves. For solving the resulting constrained optimization problems, we used the MATLAB (The MathWorks) SQP-type routine *fmincon*. In a preliminary step, initial guesses were produced by the use of the genetic algorithm type routine *ga*. Derivatives of the Tikhonov functional, needed for providing gradient information, were calculated based on eigenvalue sensitivities to avoid error-prone finite differences (see supplemental text). The optimization problems were independently solved several times to avoid the return of only local minimizers.

For the components q_i of the identified parameter vector, a 0.95 marginal confidence interval was calculated according to

$$q_j \pm \frac{\sqrt{\|data - simulation(q)\|^2}}{\sqrt{N-8}} \sqrt{(X^T X)^{-1} t(N-8, 0.05/2)}, \quad (1.6)$$

where X is simulation, (q) denotes the Jacobian matrix of the (nonlinear) simulation mapping, N denotes the total number of data points, and $t(N-8, 0.05/2)$ is the upper 0.005/2 quantile for Student's t distribution with $N-8$ degrees of freedom (Bates and Watts, 1988). Again, straightforward adaptations apply to the case of datasets corresponding to multiple mutations.

Simulation of current traces

Currents were simulated by solving the ordinary differential equation (ODE) system (Eq. 4.5) describing the four-state model (see also Supplemental Material, Part 3) making use of the estimated rate constants. Initial conditions: (1) for activation traces: steady-state distribution of channels between states at holding potential; and

(2) for deactivation traces: calculated fractions at the end of 20-ms conditioning pulse (0 mV for wild-type, -30 mV for I781G, and -40 mV for I781P). Currents were simulated using a reversal potential of 48 mV assuming a linear I-V relationship.

Online supplemental material

The time constant of current activation (Eq. 2.2) in terms of a serial three-state model (Scheme 1), a link between the steady-state activation curve (m_∞) and the fraction of open channels, the ODEs describing the four-state model, and the calculation of eigenvalue sensitivities are given in the Supplemental material, Parts 1–4, respectively. It is available at <http://www.jgp.org/cgi/content/full/jgp.200910272/DC1>.

RESULTS

Glycine mutations in the lower third of IIS6

Our previous studies provided evidence that the conserved LAIA motif in segment IIS6 of $Ca_v1.2$ is highly sensitive to proline substitutions. A proline in an α helix causes a kink of $\sim 26^\circ$ (Barlow and Thornton, 1988; Cordes et al., 2002), comparable to the 30° bend of the “glycine hinge” in the crystal structure of MthK (Jiang et al., 2002). We have, therefore, hypothesized that in $Ca_v1.2$, helix bending at these positions may play a role in activation gating (Hohaus et al., 2005). To gain further insights into the role of helix flexibility in channel gating, we substituted the LAIA motif and neighboring positions by flexible glycines. I781G induced significant changes in channel activation (Table I; compare with Hohaus et al., 2005). Fig. 2 illustrates the deactivation kinetics of wild type, A780G, and I781G at different voltages. The time constants of activation and deactivation and steady-state activation curves of wild-type, the glycine mutants (Table I), and previously described IIS6 mutants (see Hohaus et al., 2005) are shown in Figs. 3 and 8. Comparing the gating changes induced by glycine mutations with previous data of Hohaus et al. (2005) revealed no peculiarities; larger shifts of the activation curves were accompanied by slower current kinetics (see Fig. 6 C).

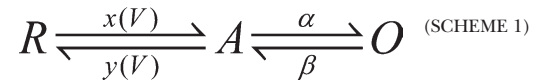
TABLE I
Midpoints and slope factors of the activation curves
of $Ca_v1.2$ IIS6 mutants

Mutant	Half-activation	Slope
	mV	mV
Wild-type ^a	-9.9 ± 1.1	6.3 ± 0.7
A780P ^a	-37.1 ± 0.7	5.7 ± 0.8
A780G	-19.3 ± 0.8	6.3 ± 0.6
I781P ^a	-47.2 ± 1.1	6.3 ± 0.6
I781G	-40.2 ± 0.8	7.5 ± 0.7
I781T ^a	-37.7 ± 1.2	7.2 ± 1.0
A782P ^a	-35.7 ± 1.4	9.8 ± 0.3
A782G	-22.2 ± 0.4	7.8 ± 0.4
V783G	No current	No current
D784G	-15.6 ± 1.1	6.3 ± 0.6

^aData from Hohaus et al. (2005).

Three-state model failed to describe both activation and deactivation

To obtain insights into mutation-specific gating modifications, we quantified current kinetics and steady-state activation curves. In a first attempt, we described $Ca_v1.2$ activation by:



This three-state model is a simplification of more complex state diagrams (see Marks and Jones, 1992; Zagotta et al., 1994a,b). Multiple voltage sensor transitions occurring before channel opening cannot be resolved from predominantly monoexponential Ca_v activation. We have, therefore, lumped together these transitions. In the resulting Scheme 1, a membrane depolarization initiates voltage sensor movement (transition $R \leftrightarrow A$ with voltage-dependent rate constants $x(V)$ and $y(V)$), which subsequently initiates a voltage-independent pore opening (transition $A \leftrightarrow O$ with rate constants α and β ; see also Marks and Jones, 1992; Zagotta et al., 1994a,b; Yifrach and MacKinnon, 2002). Thus, mechanistically the model assumes two functionally distinct channel parts: a voltage-sensing unit and a pore that opens and closes with voltage-independent rates. The rate constants of the voltage-sensing machinery are described by simple exponential functions (Eyring expressions):

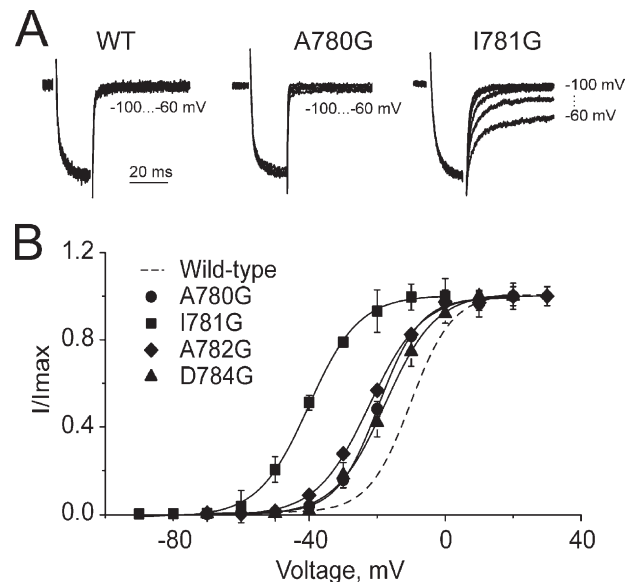


Figure 2. Glycine mutations in IIS6 differentially modulate $Ca_v1.2$ gating. (A) Representative tail currents of wild-type, A780G, and I781G channels. Currents were activated during a 20-ms conditioning depolarization to 0 mV for wild-type, -10 mV for A780P, and -30 mV for I781G. Deactivation was recorded during subsequent repolarizations (10-mV increments) starting from -100 mV. (B) Voltage dependences of steady-state activation of the indicated glycine mutants.

$$x(V) = x_0 \cdot \exp\left(\frac{V}{k_x}\right) \text{ and } y(V) = y_0 \cdot \exp\left(-\frac{V}{k_y}\right). \quad (2.1)$$

This yields the voltage dependence of time constant (see supplemental text, Part 1):

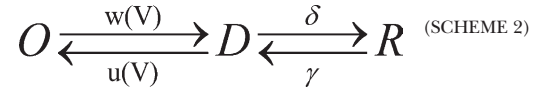
$$\tau_{act} = \frac{1}{\frac{(\alpha + \beta + x + y)}{2} \cdot \left\{ 1 - \sqrt{1 - \frac{4(\alpha \cdot x + \beta \cdot x + \beta \cdot y)}{(\alpha + \beta + x + y)^2}} \right\}} \quad (2.2)$$

The backward pathway of Scheme 1 failed, however, to describe the acceleration of deactivation at more negative voltages. In such a scenario, the channel would have to close by transition $O \rightarrow A$ before returning to the resting state ($A \rightarrow R$). If strong hyperpolarization accelerates the downward movement of voltage sensor ($y(V) \rightarrow \infty$), then voltage-independent pore closure serves as the rate-limiting stage preventing acceleration of deactivation. At negative potentials ($V < -80$ mV) this predicts a time

constant $\tau(V) \rightarrow \frac{1}{\beta}$ (deduced from Eq. 2.2) that does not reproduce our experimental findings (see Fig. 7).

Four state model for $Ca_v1.2$ activation and deactivation

We propose, therefore, a scenario for channel deactivation where channel closure is initiated by return of the voltage sensor to its resting position during hyperpolarization via a deactivated open state D:



with corresponding Eyring expressions:

$$u = u_0 \exp\left(\frac{V}{k_x}\right) \text{ and } w = w_0 \exp\left(-\frac{V}{k_y}\right). \quad (3.1)$$

Identical steepness factors (k_x and k_y) were assumed for rate constants describing the upward ($x(V)$ and $u(V)$) and downward ($y(V)$ and $w(V)$) movements of the voltage sensor. The resulting circular four-state model with separate activation (predominantly via state A) and deactivation (predominantly via state D) pathways is shown in Fig. 1. The destination point of the activation process (state O) is the departure point for deactivation and vice versa. All rate constants are linked by the thermodynamic reversibility condition at all voltages:

$$\frac{x(V)}{y(V)} \cdot \frac{\alpha}{\beta} \cdot \frac{w(V)}{u(V)} \cdot \frac{\delta}{\gamma} = 1. \quad (3.2)$$

Taking into account Eqs. 2.1 and 3.2, the thermodynamic reversibility condition can be reduced to:

$$\frac{x_0}{y_0} \cdot \frac{\alpha}{\beta} \cdot \frac{w_0}{u_0} \cdot \frac{\delta}{\gamma} = 1 \text{ or } \frac{w_0}{u_0} = \frac{\left(y_0 \cdot \frac{\beta}{\alpha}\right)}{\left(x_0 \cdot \frac{\delta}{\gamma}\right)}$$

Finally, we assumed a link between the voltage-sensing machinery and pore stability. w_0 is linked to the stability of the open state O, and u_0 is linked to the stability of open state D:

$$w_0 = y_0 \cdot \frac{\beta}{\alpha}$$

$$u_0 = x_0 \cdot \frac{\delta}{\gamma}$$

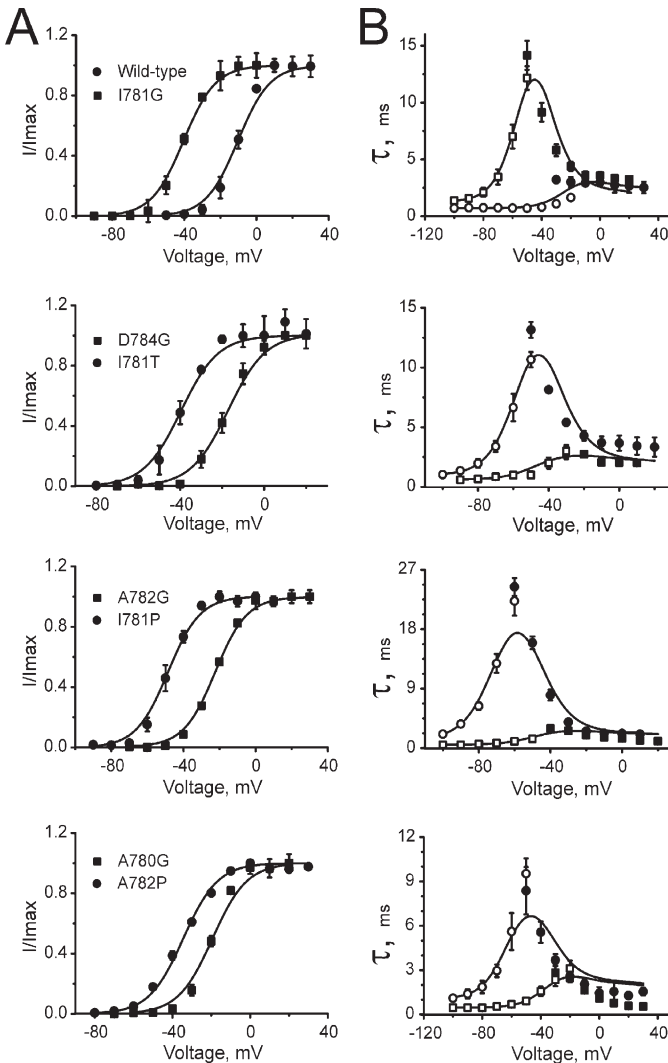


Figure 3. Effects of pore mutations on steady-state activation and current kinetics. Voltage dependences of steady-state activation (A), time constants of activation (B; filled symbols), and deactivation (B; open symbols) of the indicated channel construct. Solid lines represent model simulations based on the identified model parameters given in Tables II and III.

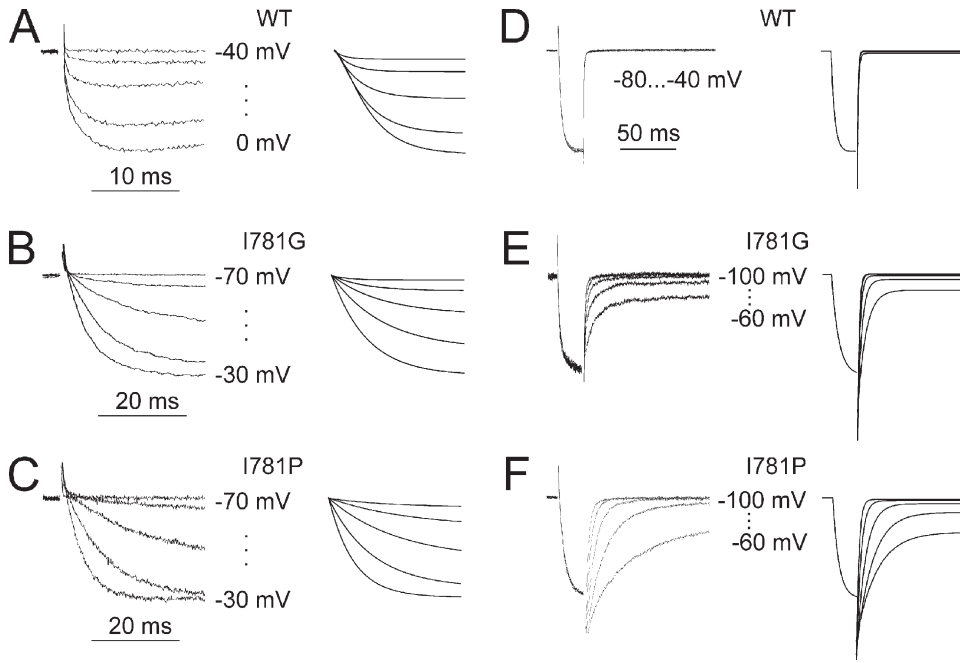


Figure 4. Recorded and simulated currents. (A–C) I_{Ba} through wild-type (A), I781G (B), and I781P (C) channels (left column) during depolarization from -80 mV to the indicated voltages and corresponding current simulations (right column). (D–F) Representative tail currents of wild-type (D), I781G (E), and I781P (F) channels (left column) and corresponding simulations (right column). The fast phase of the tail current (D–F) containing fast (not resolved) components of current deactivation is truncated. The simulated currents were calculated from the full four-state model by solving the ODE system (Eq. 4.5) making use of the estimated rate constants (Tables II and III) and a reversal potential of 48 mV (see also Materials and methods).

The voltage dependence of steady-state activation Hodgkin and Huxley (1952) introduced the term activation (m) varying from 0 to 1 to characterize the voltage dependence of normalized peak sodium conductance. In frame of the four-state model shown in Fig. 1, the fraction of open channels varies from $F_{open,min}$ at hyperpolarizing voltages to $F_{open,max}$ at depolarizing voltages. The standard activation curve is thus defined by:

$$m_{\infty} = \frac{F_{open} - F_{open,min}}{F_{open,max} - F_{open,min}} \quad (0 < m_{\infty} < 1), \quad (4.1)$$

yielding (see supplemental text, Part 2) the Boltzmann distribution:

$$m_{\infty} = \frac{1}{1 + \exp\left(\frac{V_m - V}{k_S}\right)}, \quad (4.2)$$

with midpoint

$$V_m \approx V_X - k_S \cdot \ln\left(1 + \frac{\alpha}{\beta}\right) \quad (4.3)$$

TABLE II
Rate constants of $A \leftrightarrow O$ and $R \leftrightarrow D$ transitions (in ms^{-1})

Construct	α	β	γ	δ
Wild-type ^a	0.15 ± 0.11	0.24 ± 0.08	0.021 ± 0.021	1.39 ± 0.17
G770P	0.33 ± 0.31	0.31 ± 0.21	0.030 ± 0.073	0.56 ± 0.11
N771P ^a	0.95 ± 0.63	0.11 ± 0.07	0.111 ± 0.057	1.41 ± 0.23
F778P ^a	0.13 ± 0.12	0.28 ± 0.09	0.016 ± 0.026	0.70 ± 0.09
L779P ^a	1.79 ± 0.81	0.11 ± 0.02	0.002 ± 0.002	0.36 ± 0.09
A780P ^a	0.19 ± 0.03	0.0064 ± 0.0022	0.015 ± 0.005	0.14 ± 0.02
A780G	0.96 ± 0.62	0.27 ± 0.12	0.037 ± 0.022	2.10 ± 0.33
I781T ^a	1.95 ± 0.91	0.045 ± 0.012	0.009 ± 0.003	1.02 ± 0.26
I781P ^a	4.16 ± 1.86	0.034 ± 0.007	0.003 ± 0.001	0.74 ± 0.43
I781G	1.73 ± 0.81	0.036 ± 0.010	0.011 ± 0.003	0.78 ± 0.18
I781A ^a	1.72 ± 0.79	0.132 ± 0.028	0.003 ± 0.001	1.55 ± 0.44
I781V ^a	0.55 ± 0.30	0.22 ± 0.03	0.0003 ± 0.0002	2.01 ± 0.77
I781N ^a	2.17 ± 0.99	0.10 ± 0.02	0.003 ± 0.002	0.74 ± 0.20
A782P ^a	2.65 ± 1.23	0.111 ± 0.026	0.004 ± 0.002	0.94 ± 0.27
A782G	1.74 ± 0.97	0.32 ± 0.10	0.013 ± 0.009	1.96 ± 0.37
D784G	0.88 ± 0.53	0.34 ± 0.09	0.008 ± 0.006	1.62 ± 0.35

^aRate constants estimated using data from Hohaus et al. (2005).

TABLE III

Model parameters describing the $R \leftrightarrow A$ transition

Rate constant	Estimated value
x_0 (ms^{-1})	0.427 ± 0.029
k_x (mV)	328.8 ± 447.4
y_0 (ms^{-1})	0.216 ± 0.084
k_y (mV)	9.04 ± 0.52

and a slope factor

$$k_S = \frac{k_x \cdot k_y}{k_x + k_y} \text{ and } V_X = k_S \cdot \ln\left(\frac{y_0}{x_0}\right). \quad (4.4)$$

This expression illustrates that the slope of the activation curves does not depend on pore stability (α , β , γ , and δ).

The voltage dependence of the time constant τ

The linear ODE describing the circular four-state model of Fig. 1

$$\begin{cases} \frac{dR}{dt} = -x \cdot R + y \cdot A - \gamma \cdot R + \delta \cdot D \\ \frac{dA}{dt} = x \cdot R - y \cdot A - \alpha \cdot A + \beta \cdot O \\ \frac{dO}{dt} = \alpha \cdot A - \beta \cdot O - w \cdot O + u \cdot D \\ R + A + O + D = 1 \end{cases} \quad (4.5)$$

can in vectorial notation be compactly written as

$$\frac{dS}{dt} = MS + b,$$

with state vector $S = (R, A, O)$, the vector $b = (\delta, 0, u(V))$, and the matrix M as given in (Eq. S10).

The time constants τ recorded at various voltage values can be described by

$$\tau = -1 / \lambda_{\min}(V, q), \quad (4.6)$$

where λ_{\min} denotes the smallest eigenvalue of the matrix M .

The eigenvalues of this matrix are real, negative, and distinct (for physically meaningful parameters), such that λ_{\min} is well defined (see Hearon, 1953). Two other (larger)

eigenvalues correspond to early current activation phases that were not resolved in our experiments (see Materials and methods). The simulation of the time constant data requires the computational determination of λ_{\min} , based on the eigenvalue equation

$$M \cdot v_{\min} = \lambda_{\min} \cdot v_{\min}, \quad (4.7)$$

for which numerical routines are available in MATLAB or related software packages.

Determination of model parameters for individual mutants
First, we applied the inverse problem approach to estimate the rate constants of $\text{Ca}_v1.2$ activation and deactivation for individual IIS6 mutants. Corresponding parameters for channel construct I781T are exemplified in Table IV. The large confidence intervals of the estimated rate constants illustrate that traditional measures of calcium current kinetics and steady state do not provide sufficient information for parameter identification in frame of the gating model illustrated in Fig. 1.

Estimation of rate constants for a large set of $\text{Ca}_v1.2$ mutants

Next, we reduced the dimension of the parameter search space by assuming that pore mutations are unlikely to significantly affect the voltage-sensing machinery (see also Yifrach and MacKinnon, 2002). Rate constants α , β , γ , and δ for wild-type and all IIS6 mutants were thus estimated with identical $x(V)$ and $y(V)$. As evident from Figs. 3 and 8 and Tables II and III, the steady-state activation curves and current kinetics of 15 constructs were fitted by the model with narrower confidence intervals. Fig. 4 displays simulated current kinetics for wild-type $\text{Ca}_v1.2$ and mutants I781G and I781P, making use of the estimated rate constants that are given in Tables II and III.

Specific gating behavior of mutant A780P

Fitting A780P with $x(V)$ and $y(V)$, common for all mutants, failed to reproduce simultaneously steady-state activation and time constants of activation and deactivation. This is evident from Fig. 5 B, where the predicted activation time constant in the voltage range between -40 and -20 mV was approximately two times larger than the experimental values. Furthermore, fitting constraint (Eq. 1.5; see Materials and methods) was active,

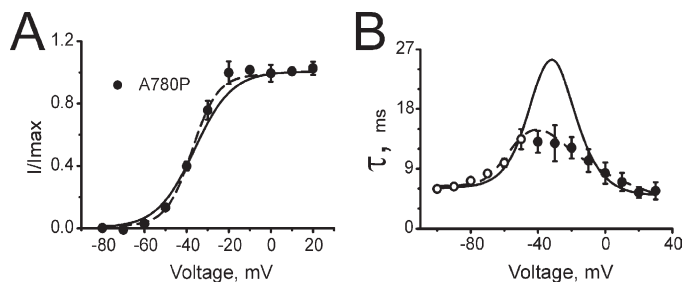


Figure 5. Steady-state activation and current kinetics of A780P. Voltage dependence of steady-state activation (A) and time constants of activation and deactivation (B) of mutant A780P. Solid lines show simulations based on the rate constants $x(V)$ and $y(V)$ of Table III. Voltage dependence of the activation time constants (B) was not reproduced under the assumption of $x(V)$ and $y(V)$ being identical for all mutants. Dotted lines show improved simulations for A780P obtained by individual fits of $x(V)$ and $y(V)$ (see Table IV).

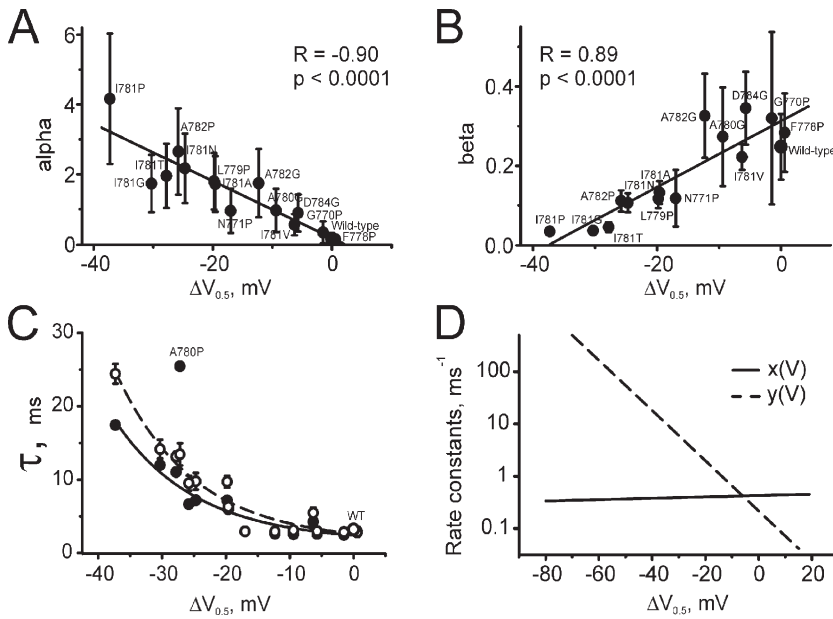


Figure 6. Rate constants of channel opening and closure. (A and B) Correlations between estimated rate constants of opening (A) and closure (B) and shifts of the activation curves ($\Delta V = V_{1/2, \text{MUT}} - V_{1/2, \text{WT}}$) for IIS6 mutations. (C) Maximal time constants experimentally measured (open circles) and calculated (filled circles; see bell-shaped curves in Figs. 3 and 8) versus corresponding shifts of the activation curves. Lines represent fits by monoexponential functions ($A_0 + A_1 * \exp(-\Delta V/k)$), with $A_0 = 1.57 \pm 1.10$, $A_1 = 1.09 \pm 0.52$, and $k = 12.2 \pm 1.9$ for experimental data, and $A_0 = 1.53 \pm 0.95$, $A_1 = 0.88 \pm 0.49$, and $k = 12.7 \pm 2.3$ for calculated data. (D) Voltage dependence of $x(V)$ and $y(V)$ plotted in semilogarithmic scale. $x(V)$ represents the voltage dependence of the forward rate and $y(V)$ the backward movement of the voltage-sensing machinery (see Fig. 1). A steeper voltage dependence of $y(V)$ is evident.

indicating that the model paradigms conflict with the gating characteristics of A780P.

Changes in $x(V)$ and $y(V)$ significantly improved the quality of the fit. The dashed line in Fig. 5 B represents a simulation for A780P kinetics with $x(V)$ and $y(V)$ that was obtained from an individual fit (Table III). These data suggest that the hypothesis that pore mutations do not significantly affect the voltage sensing machinery is not fulfilled for all mutations.

Inverse relation between channel opening and closure rates

Fig. 6 (A and B) displays the relation between the estimated rate constants of opening and closure (α and β) and the corresponding shifts of the activation curves. Larger shifts in steady-state activation are accompanied by an increase in α (reflecting a destabilization of the closed pore) and a decrease in β (reflecting a stabilization of the open-channel conformation). Both trends were statistically significant (Fig. 6, A and B). The rates of voltage-independent (spontaneous) channel openings (γ) from the resting state R are given in Table II together with the rates of channel closure δ . No correlations with shifts were found either for γ or for δ (not depicted).

Relation between current deceleration and shift of the activation curve

The shifts of the steady-state activation curves versus the estimated maximal time constants (peaks of the bell-shaped dependencies in Figs. 3 and 8) are plotted in Fig. 6 C. Larger shifts of the activation curve were typically associated with a gradual deceleration of current kinetics. The data of A780P did not fit this relationship, highlighting peculiarities in the gating of this mutant.

Fig. 6 D shows the voltage-dependent rate constants $x(V)$ and $y(V)$ in semilogarithmic scale (see also Table III).

DISCUSSION

We have previously shown that amino acid substitutions in the lower third of segment IIS6 of $\text{Ca}_v1.2$, and in particular the substitution of I781 by residues of different hydrophobicity, size, and polarity, shift the voltage dependence of activation toward more negative potentials (Hohaus et al., 2005; Raybaud et al., 2006; Hering et al., 2008).

Here, we extended this analysis by introducing glycine mutations to evaluate the role of helix flexibility. Substitution of I781 by glycine induced slow activation and deactivation kinetics and a substantial shift of the activation curve ($\Delta V_{\text{act}} = -30$ mV). Other glycine mutations affected kinetics to different extents and induced, compared with

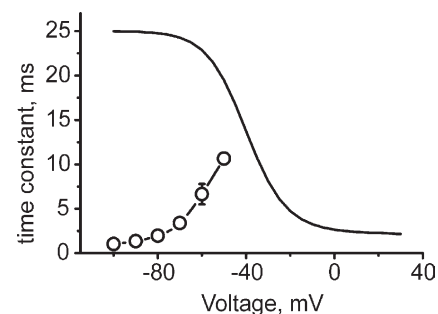


Figure 7. Voltage dependence of deactivation time constants predicted by fitting the data for mutant I781T to the backward activation pathway: $O \rightleftharpoons A \rightleftharpoons R$. Deactivation time constant (solid line) was calculated by Eq. 2.2 (rate constants are indicated in Tables II and III). The model predicts an increase of the deactivation time constants, whereas the experimentally measured time constants decreased with increasing hyperpolarization (open circles connected by broken line).

the strong gating perturbations induced by I781P/T, less pronounced shifts of the activation curves (I781P > I781G > I781T > A782G > A780G > D784G; Table I and Figs. 2 and 3; compare with Fig. 8). Mutation I781G thus confirmed the previously established particular gating-sensitive position I781 (Hohaus et al., 2005; see also Kudrncac et al., 2009). In general, glycine substitutions and other IIS6 mutations in $Ca_v1.2$ induced either negligible changes (e.g., G770P; Hohaus et al., 2005) or substantial shifts in channel gating accompanied by a deceleration of activation kinetics. Collectively, these and previous data revealed a link between deceleration of current kinetics and the gradual leftward shift of the activation curve (Fig. 6 C). Double mutants in neighboring amino acids in IS6 and IIS6 confirmed this trend (Kudrncac et al., 2009).

In potassium channels (Yifrach and MacKinnon, 2002) and NaChBac (Zhao et al., 2004), similar shifts of the activation curves were explained by a destabilization of the closed and/or a stabilization of the open-channel conformation without a perturbation of the voltage-sensing machinery. In the present study, we evaluated this paradigm for $Ca_v1.2$.

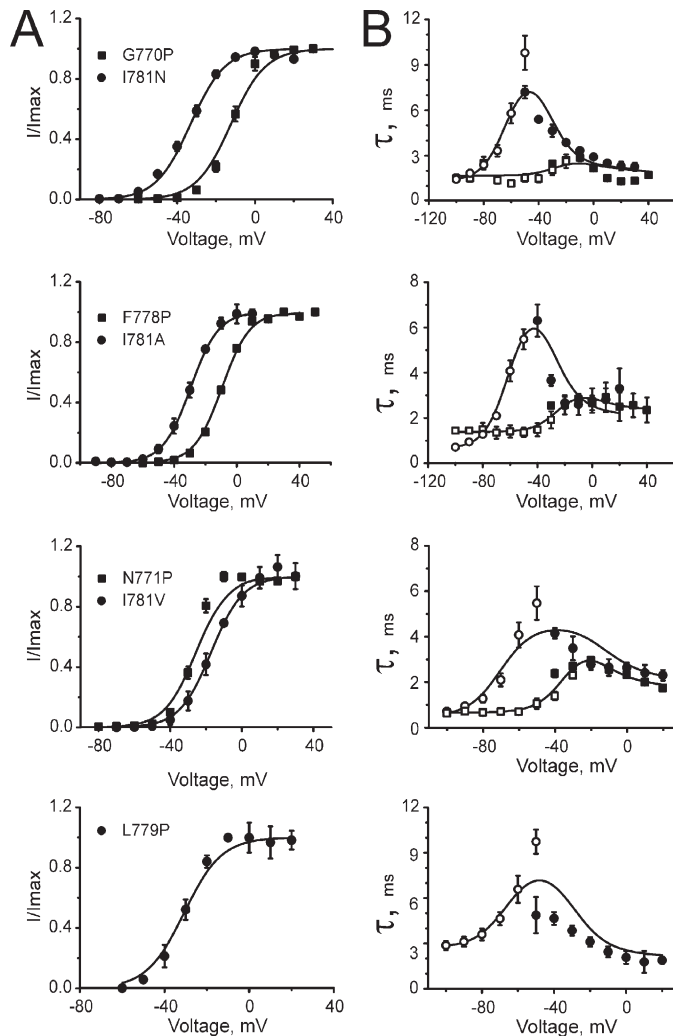


TABLE IV
Individually fitted model parameters for I781T and A780P

Rate constants	I781T	A780P
x_0 (ms^{-1})	0.279 ± 0.026	0.116 ± 0.035
k_x (mV)	214.0 ± 330.5	62.2 ± 36.1
y_0 (ms^{-1})	0.056 ± 2.607	0.023 ± 15.695
k_y (mV)	6.65 ± 0.05	7.15 ± 0.08
α (ms^{-1})	6.8 ± 315.0	4.3 ± 2962.6
β (ms^{-1})	0.072 ± 0.015	0.063 ± 0.021
γ (ms^{-1})	0.0027 ± 0.0020	0.0021 ± 0.0203
δ (ms^{-1})	0.858 ± 0.107	0.153 ± 0.028

A minimal model for $Ca_v1.2$ activation and deactivation

To quantify the underlying gating perturbations, we first exploited a serial three-state model (Scheme 1) with voltage-independent rate constants of pore opening and closure (α and β). This gating scheme predicts increasing deactivation time constants with hyperpolarization, which is in contradiction to our experimental findings (Fig. 7). Therefore, to fit our data we designed a more complex, circular four-state model (Fig. 1), where $Ca_v1.2$ channels can activate and deactivate via different pathways. Both processes are initiated by voltage sensor movements. During activation the voltage sensor moves in response to a depolarization from a “gate-locking position” R to A (where the channel is still closed) with voltage-dependent rate constants $x(V)$ and $y(V)$. The unlocked channel opens with a rate constant α and closes with a rate constant β (Fig. 1). During deactivation the voltage sensor moves toward the “gate-locking position.” If channels sojourned in state A (activated/closed), they return to the resting state R. If channels were open, they enter the state D and subsequently close by returning to R.

Inverse problem approach for parameter identification

After an inverse problems approach, we determined: (1) the rate constants ($x(V)$ and $y(V)$) of the transitions of the voltage-sensing machinery from the resting to the activated state, and (2) the rate constants of pore opening and closure (α , β , γ , and δ). However, the application of this approach to individual channel mutants provided satisfactory fits with large confidence intervals (Table IV). Assuming that the rate constants $x(V)$ and $y(V)$ are identical for all mutants allowed the identification of all rate constants with narrower confidence intervals (Figs. 3 and 8, and Tables I and II). This approach enabled us to fit the kinetics of 15 out of 16 channel constructs (Figs. 3 and 8). Simulations of current kinetics with estimated

Figure 8. Steady-state and kinetic characteristics of previously described mutants (Hohaus et al., 2005). Voltage dependencies of steady-state activation (A), time constants of activation (B; filled symbols), and deactivation (B; open symbols) of the indicated constructs. Solid lines represent the simulations based on the model parameters identified (see Tables II and III).

rate constants exemplified for wild type, I781G, and I781P (Fig. 4) illustrate the quality of the fit.

Particular effect of mutation A780P

Clear discrepancies between predicted and experimental data for mutant A780P are illustrated in Fig. 5. Between -40 and -20 mV, the predicted time constants of channel activation of mutant A780P were approximately two times larger than the experimentally determined values (Fig. 5 B, solid line). Fitting the steady-state and current kinetics of A780P by the model individually led to a substantial improvement (Fig. 5, dashed lines). A trend toward stronger voltage dependence of $x(V)$ was observed (compare k_x in Table IV with k_x of all other mutants given in Table III). We speculate that substitution of A780P in segment IIS6 of $Ca_v1.2$ significantly affects the interaction between the voltage-sensing machinery and the channel pore. Rigid helix bending in position A780 might be directed toward the voltage-sensing structures, leading to restricted mobility of the voltage-sensing domain ("sensor clip"). Hence, the introduction of a flexible glycine into this position induced only an ~ 10 -mV shift of the activation curve without significantly changing current activation and deactivation kinetics (A780G; Figs. 2 and 3).

Weak voltage dependence of pore-releasing sensor transition

The voltage dependences of $x(V)$ and of $y(V)$ obtained for the other 15 constructs are shown in Fig. 6 C. Steeper dependence of $y(V)$ on voltage (with $k_y = 9.04 \pm 0.52$ mV) compared with the "gate-releasing" movement (with a $k_x = 328 \pm 447$ mV) indicates that changes in membrane voltage are more efficient in closing than in opening the channel. The weak voltage dependence of $x(V)$ prevented a precise estimation of its steepness factor k_x (wide confidence interval). Indeed, if current activation is determined largely by $y(V)$, changes in $x(V)$ have a minor (and hardly detectable) influence. Weak voltage dependence of the forward rate constant of the voltage-sensing unit ($x(V)$) versus the strong voltage dependence of the backward transition ($y(V)$) suggests that the membrane voltage is more efficient in forcing the $Ca_v1.2$ into a closed state than "pulling" the gate open (Fig. 6 D), which is in line with previous observations on voltage-gated potassium channels (for review see Fedida and Hesketh, 2001).

Stabilization of the open- or destabilization of the closed-channel pore?

The majority of IIS6 mutations analyzed in this and a previous paper (Hohaus et al., 2005) shift the activation curve to more hyperpolarized voltages. These changes in steady-state activation reflect either a destabilization of the closed state and/or a stabilization of the open-channel conformation (Yifrach and MacKinnon, 2002; Zhao et al., 2004). Compared with previous studies, our analysis accounted for steady-state and kinetic data simultane-

ously. A trend that mutations in the lower part of IIS6 destabilizing the closed state stabilize the open state is evident (Fig. 6, A and B). This observation is an interesting finding per se and suggests a structural link between both conformations of $Ca_v1.2$ that has yet to be identified.

This study was supported by a grant from The Austrian Science Fund (FWF; Project P19614-B11).

Angus C. Nairn served as editor.

Submitted: 5 June 2009

Accepted: 29 July 2009

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